

# Reflection, Transmission and Fresnel's Coefficients\*

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Brewster's angle is the angle of incidence at which **p** polarized light is perfectly transmitted through a transparent dielectric surface such as glass, without any reflection. In this experiment, you will find the Brewster's angle by measuring the reflectance of a glass slide for **p** polarized light. You will also measure the reflectance for **s** polarized light and light polarized at  $45^\circ$  with respect to the incidence plane. Furthermore, Brewster angle will be used to calculate the refractive index of glass.

**Essential pre-lab reading:** “*Physics of Light and Optics*” by Justin Peatross and Michael Ware, Brigham Young University, 2013; (Chapter 3: Reflection and Refraction, Sections 3.1 to 3.4).

## 1 Test your understanding

1. Derive Fresnel's reflection and transmission coefficients for **s** and **p** polarized light. Let's call these coefficients  $r_s$ ,  $r_p$ ,  $t_s$  and  $t_p$ .
2. Use MATLAB (or a software of your choice) to plot the following quantities for air-glass interface as a function of the incident angle. Use  $n_i = 1$  for air and  $n_t = 1.6$  for glass.
  - (a)  $r_p$  and  $t_p$ .
  - (b)  $R_p$  and  $T_p$ , where  $R_p = r_p^*r_p$  and  $T_p = t_p^*t_p$ .
  - (c)  $r_s$  and  $t_s$ .
  - (d)  $R_s$  and  $T_s$ , where  $R_s = r_s^*r_s$  and  $T_s = t_s^*t_s$ .
3. On our website, you are provided with a simulation named *reflectance.m*, which shows the effects of changing the refractive index and the polarization on  $R$ . Use this simulation to further investigate the relation between these entities.

## 2 The Experiment

The setup includes a HeNe laser which emits unpolarized light of 633 nm wavelength. The unpolarized light passes through a linear polarizer and then a half-wave plate (HWP). Orient

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the HWP such that the light coming out of it is  $p$  polarized. To make sure that the light is  $p$  polarized, follow this technique: <https://goo.gl/zGxphV>. Now, this linearly polarized beam will pass through an iris and fall on a glass slide of some unknown Brewster angle.

**Q 1.** Why are we using an iris in this setup?

This glass slide is mounted on the second level of a two-level rotation mount. The reflected beam is measured by a photodetector which is mounted on the first level of rotation mount. The photodetector outputs current proportional to the light intensity, which is first converted to voltage by an  $I$ - $V$  converter and then displayed on a multimeter, as shown in Figure 1.

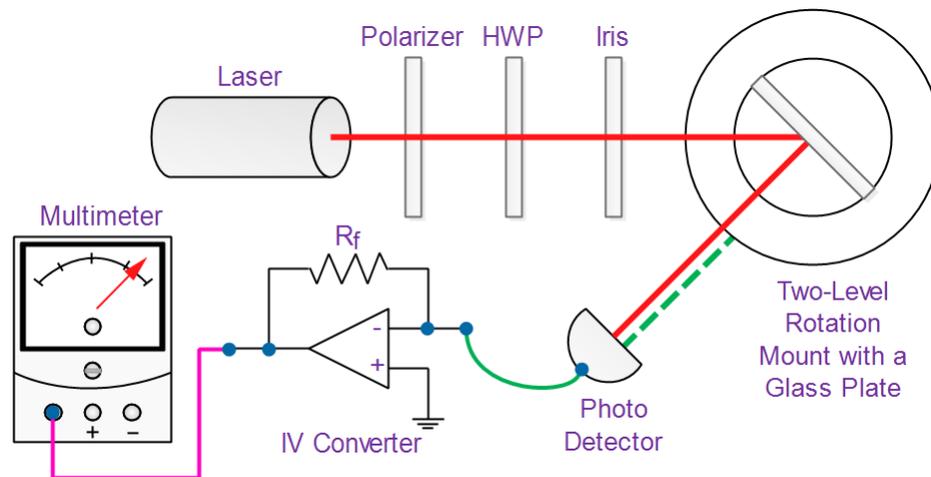


Figure 1: Schematic of the experimental setup. The red line represents the conceived path of the laser beam.

**Q 2.** Using the arrangement of Figure 1, find the reflectance curve for  $p$  polarized light and use it to determine the Brewster angle. Determine the uncertainty as well.

Orient the HWP to obtain  $s$  polarized light and then, in another experiment,  $45^\circ$  linearly polarized light. If the incident linear polarization makes an angle  $\theta$  with the *fast axis* of the HWP, the polarization of the outgoing beam is rotated by  $2\theta$ . Therefore, you can now obtain  $s$  or  $45^\circ$  polarizations from  $p$  polarized light by rotating the HWP through  $45^\circ$  or  $22.5^\circ$  respectively.

**Q 3.** Find the reflectance curves for  $45^\circ$  linearly polarized and  $s$  polarized light.

**Q 4.** Why are we using a HWP and not just rotating the polarizer to achieve the required polarization state?

**Q 5.** Reflectance can only have values from zero to one. Therefore you need to normalize your data. At some suitable angle (e.g.  $20^\circ$ ), use the theoretically calculated value to normalize your data. Then plot your results superimposed with theoretically calculated curves. Include uncertainty bars with your data.

**Q 6.** Find Brewster's angle and refractive index of the glass sample. Quote the uncertainty in your results.